

# Maths Knowledge Organiser

## Year 9 Area, surface area and volume



### Area

Area is the space inside a 2D shape

$\text{Area} = \pi \times r^2$   
 $\text{Circumference} = \pi \times d$

A compound shape is a 2D shape made up of simpler shapes

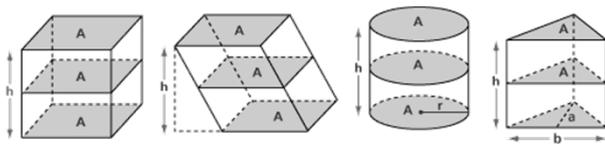
We work out its area by breaking them up and working out separate areas

(1)  $3 \times 3 = 9 \text{ cm}^2$   
 (2)  $9 \times 5 = 45 \text{ cm}^2$   
 $45 + 9 = 54 \text{ cm}^2$

### Volume - prisms

Is the space inside a 3D shape

A prism has a constant cross section, work out its area and multiply by length



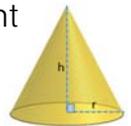
### Surface area - prism

Is the total area of each individual face of a 3d shapes

$\text{Surface Area} = 2lw + 2lh + 2wh$

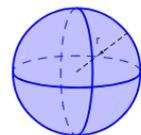
### Volume - pyramids and cones

As this is not a prism it has a different formula:  $\frac{1}{3} \times \text{area of base} \times \text{height}$



### Volume - spheres

As this is not a prism it has a different formula:  $\frac{4}{3} \times \pi \times r^3$

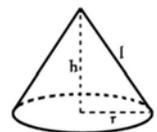


### Surface area - cone

Area of the circle plus the curved surface

You may have to use Pythagoras

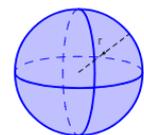
The formula:  $\pi r^2 + \pi r l$



### Surface area - sphere

Amazingly the surface area of a sphere is 4 circles

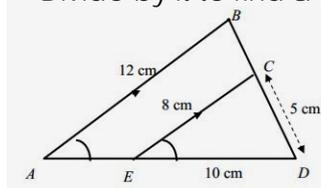
The formula:  $4\pi r^2$



### Similar shapes - lengths

Always divide 2 corresponding values to find the scale factor then

- Multiply by it to find a larger value
- Divide by it to find a smaller value



To calculate the length BC

$$SF = \frac{12}{8} = 1.5$$

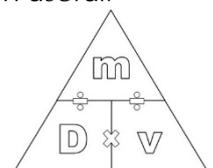
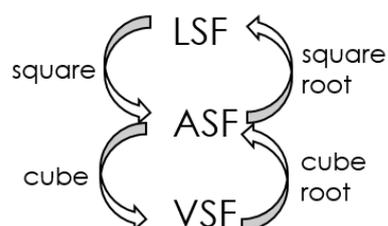
$$5 \times 1.5 = 7.5$$

$$7.5 - 5 = 2.5 \text{ cm}$$

### Similar shapes - lengths, area and volumes

When a problem involves length, area and volume you may have to change the scale factor.

LSF = length scale factors  
 ASF = area scale factors  
 VSF = volume scale factor

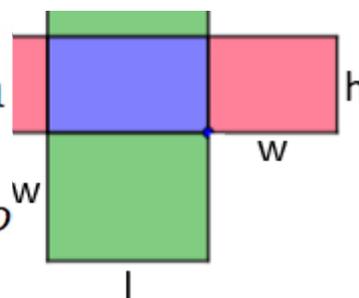
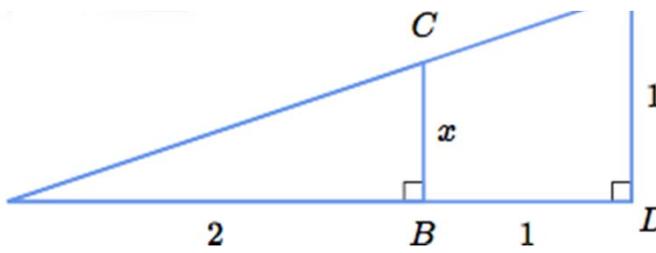


### Density

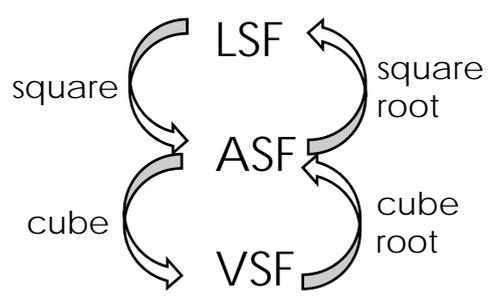
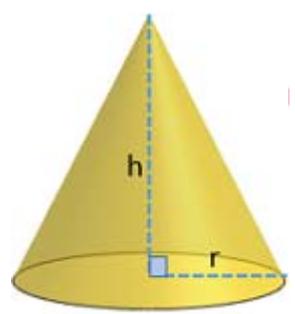
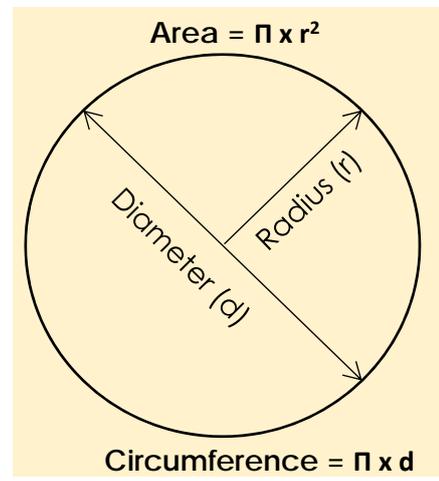
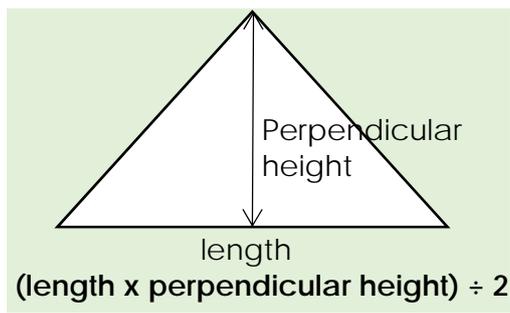
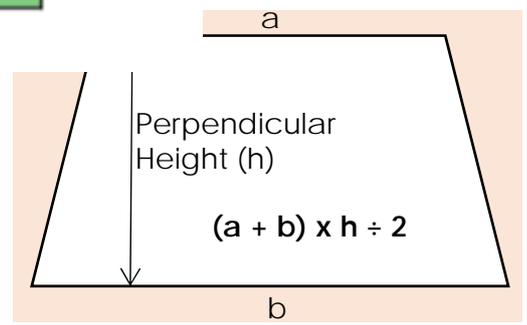
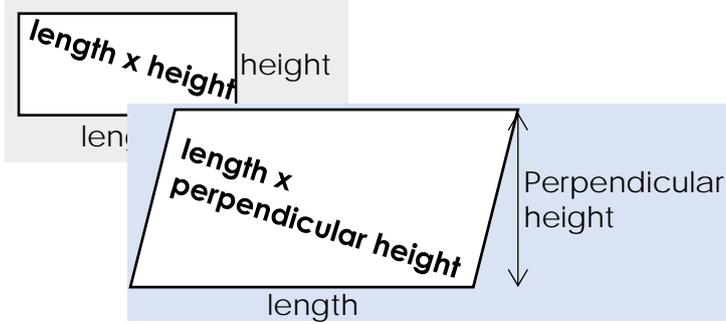
the degree of compactness of a substance.

The formula:  $\text{density} = \frac{\text{mass}}{\text{volume}}$

A formula triangle is often useful:



**A** Surface Area =  $2lw + 2lh + 2wh$   
 Area is the space inside a 2D shape



Calculate the area of rectangles, triangles and compound shapes
Calculate the area of a trapezium
Calculate the area of a circle
Calculate the area of compound shapes
Solve contextual area problems
Calculate the volume of a prism (cubes, cuboids)
Calculate the volume of a square based pyramid
Calculate the volume of a sphere
Calculate the surface area of a prism
Calculate the surface area of a cone
Calculate the surface area of a sphere
Calculate missing sides of similar shapes/triangles
Calculate the areas and volume of similar shapes
Calculate densities of 3D shapes