

Maths Knowledge Organiser

Year 10 (H) Further Statistics



Population

A population is the entire pool from which a statistical sample is drawn

Census

A census is a survey conducted on the whole population

Sample

Refers to a set of observations drawn from a population

Bias

A systematic (built-in) error which makes all values wrong by a certain amount.

Cumulative frequency graphs

This is a running total of the frequency, **add** the previous frequency

Age, x years	Frequency	Cumulative frequency
20 < x ≤ 30	12	12
30 < x ≤ 40	30	42
40 < x ≤ 50	28	70
50 < x ≤ 60	22	92
60 < x ≤ 70	8	100

The last cumulative frequency should be the total

Simple random sampling

A selection that is chosen randomly (purely by chance, with no predictability)
For example picking names out of a hat

Stratified sampling

This is where we divide the population into groups (*strata*) by some characteristic such as age or occupation or gender. Then make sure the right proportion is in each group.

$$\text{Number selected from each strata} = \left(\frac{\text{strata size}}{\text{total population}} \right) \times \text{sample size}$$

Histograms

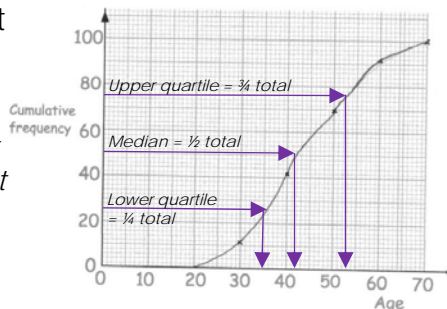
It is similar to a bar Chart, but a histogram groups numbers into ranges.

The big difference is there are **no gaps** and we use **frequency density**

$$\text{Frequency density} = \frac{\text{Frequency}}{\text{Class width}}$$

Then to plot the graph use the **upper bound** to plot

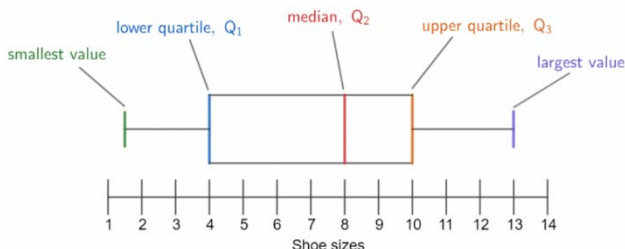
Don't forget the first point



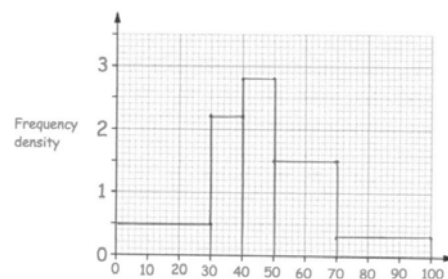
IQR Inter quartile range is the difference between the upper and lower quartile

Box plots

Get the below information and plot



Test score, x	Frequency	Frequency density
0 < x ≤ 30	15	0.5
30 < x ≤ 40	22	2.2
40 < x ≤ 50	28	2.8
50 < x ≤ 70	30	1.5
70 < x ≤ 100	9	0.3



Frequency can be calculated from histograms by the following formula

$$\text{Frequency} = \text{Frequency density} \times \text{class width}$$

Frequency can be used to work out estimates

Age, x years	Frequency	Cumulative frequency
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